# **Machine Learning Engineer Nanodegree**

## **Capstone Project Report -**

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## **I. Definition**

S&P 50 Index Price prediction through Neural networks and statistical modelling.

### **Project Overview**

To predict S&P 500 Index prices using historical data since 1871 and statistical models like Linear Regression, LSTM(Long Short-term Memory) and fbProphet.

### **Domain Background**

Domain background for this Capstone project is investment banking. The Standard & Poor's 500, often abbreviated as the S&P 500, or just the S&P,is an American stock market index based on the market capitalizations of 500 large companies having common stock listed on the NYSE or NASDAQ. The S&P 500 index components and their weightings are determined by S&P Dow Jones Indices. It differs from other U.S. stock market indices, such as the Dow Jones Industrial Average or the NASDAQ Composite index, because of its diverse constituency and weighting methodology.

This project and topic is relevant for predicting stock and index prices using AI and machine learning algorithms because this is a field where lots of data and experience are funneled and fed to different algorithm based prediction and trading. This project is another try to verify future pricing based on historical data and prediction analysis.

Personal motive for this project is to predict S&P 500 index price and to compare how various machine learning models perform in predicting price for time series data based on historical variables like sales, price, PE ratio etc with supervised learning models. Motivation is also to implement supervised learning and Neural Networks on real time dataset to check validity against market value.

I could not find any study directly applicable to the features and dataset I have selected. But below given studies are similar to what I am trying to achieve.

Reference- <http://www.diva-portal.org/smash/get/diva2:1213449/FULLTEXT01.pdf>

<https://www.kaggle.com/amarpreetsingh/stock-prediction-lstm-using-keras/notebook>

S&P 500 Index- <https://en.wikipedia.org/wiki/S%26P_500_Index>

### **Problem Statement**

Problem statement is to predict S&P 500 index price for next month and find short term trend in price movement. This is a **regression problem** based on historical data provided in time-series.

Some surveys show 30% of all stock trading done on NYSE is driven by machine learning and algorithmic models. Problem statement for this project is to verify how accurate price predictions can machine learning make based on historical monthly, quarterly and yearly data available about S&P500 index vs what has been the closing price of index. See the dataset features available in next section.

If machine learning stock trading are to be believed, then which algorithm I have selected below suits best in this given context and dataset.

Implementation strategy-

1. Data capture and data loading into master Pandas dataframe.
2. Handling missing values- Imputation and Interpolation.
3. Data Visualization and data analysis.
4. Feature Engineering.
5. Data preprocessing- Scaling.
6. Modelling and deep learning.
7. Model Evaluation Metrics

### **Metrics**

1. Mean Square Error for Linear Regression and LSTM neural network.

In regression analysis, "mean squared error" measures the mean value of the squared deviations of the predictions from the true values, over an out-of-sample test space, generated by a model estimated over a particular sample space. The MSE is a measure of the quality of an estimator—it is always non-negative, and values closer to zero are better.

is a vector of n predictions generated from a sample of n data points on all variables and Y is the vector of observed values of the variable being predicted, then the within-sample MSE of the predictor is computed as

MSE(Y, ) =

This is an easily computable quantity for a particular sample (and hence is sample-dependent).

<https://en.wikipedia.org/wiki/Mean_squared_error>.

<https://scikit-learn.org/stable/modules/model_evaluation.html#mean-squared-error>

1. R2 Score for Linear Regression and LSTM

It provides a measure of how well future samples are likely to be predicted by the model. Best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a score of 0.0.

If y^i is the predicted value of the i-th sample and yi is the corresponding true value, then the score R² estimated over nsamples is defined as

= 1- /

Where .

is the mean of observed data. <https://scikit-learn.org/stable/modules/model_evaluation.html#r2-score>

1. LSTM training accuracy, validation loss and validation accuracy-

Metrics on the training set let you see how your model is progressing in terms of it's training, but it's metrics on the validation set that let you get a measure of the quality of your model - how well it's able to make new predictions based on data it hasn't seen before.With this in mind, loss and acc are measures of loss and accuracy on the training set, while val\_loss and val\_acc are measures of loss and accuracy on the validation set.

The lower the **loss,** the better a model (unless the model has over-fitted to the training data). The loss is calculated on **training** and **validation** and its interpretation is how well the model is doing for these two sets. Unlike accuracy, loss is not a percentage. It is a summation of the errors made for each example in training or validation sets. In this problem **MSE** is the loss function as this is a regression. Then naturally, the main objective in a learning model is to reduce (minimize) the loss function's value with respect to the model's parameters by changing the weight vector values through different optimization methods, such as backpropagation in neural networks.

Loss value implies how well or poorly a certain model behaves after each iteration of optimization. Ideally, one would expect the reduction of loss after each, or several, iteration(s).

The accuracy of a model is usually determined after the model parameters are learned and fixed and no learning is taking place. Then the test samples are fed to the model and the number of mistakes (zero-one loss) the model makes are recorded, after comparison to the true targets. Then the percentage of misclassification is calculated.

Ref- <https://stackoverflow.com/questions/34518656/how-to-interpret-loss-and-accuracy-for-a-machine-learning-model>

MSE loss function for keras- <https://keras.io/losses/>

## **Analysis**

### **Data Exploration**

**Dataset-**

I have selected a dataset from Quandl.com where MULTPL provides S&P500 index related attributes for free. This data is split into monthly, quarterly and yearly basis and available through API upto latest date. Dataset is a time-series since the inception of S&P500 index in 1871. I could not find any dataset or project on Kaggle or similar websites with same dataset or with same objective. There are some stock price datasets and regression projects for predicting stock price or S&P 500 index price prediction but not on similar dataset.

Dataset info- Original data as received from Quandl API has 15.2% missing or NaN values in the time series. The reason is monthly, quarterly and year values on the time series like S&P 500 Dividend Growth by Year,S&P 500 Dividend Growth by Quarter,S&P 500 Price to Book Value by Quarter,Shiller PE Ratio by Year.

**Dataset info**:

|  |  |
| --- | --- |
| **Number of variables** | 36 |
| **Number of observations** | 3558 |
| **Total Missing (%)** | 15.2% |
| **Total size in memory** | 1000.8 KiB |
| **Average record size in memory** | 288.0 B |

Variables types -

Numeric 36

Categorical 0

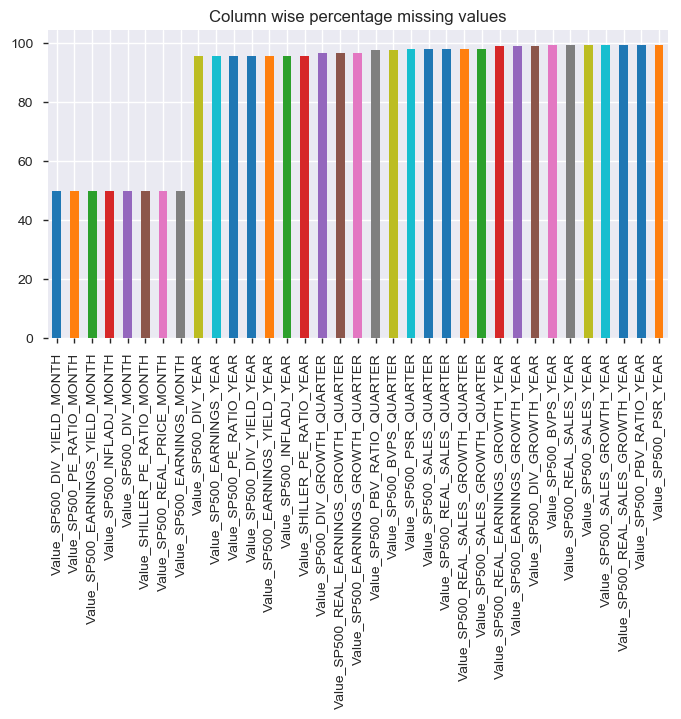
Boolean 0

Date 1

Text (Unique) 0

**NaN or missing values**-

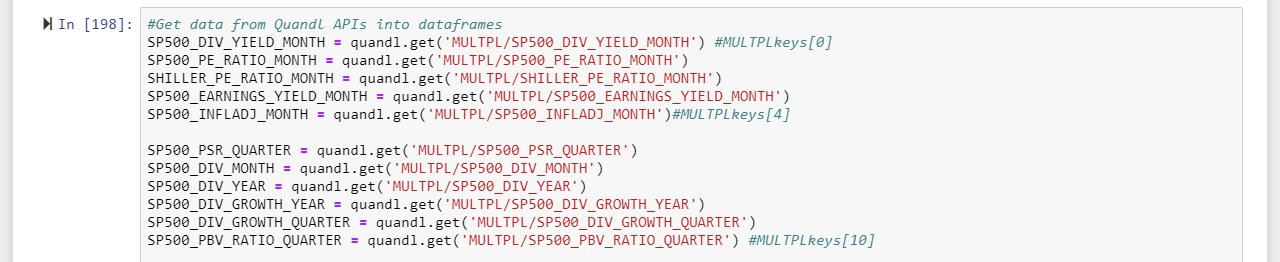
Challenge is to handle NaN values for dates where yield and ratio are not available. As depicted in the plot below, all yearly data values have more than 90% missing values are converted to np.NaN values in pandas dataframe. These NaN values would be handled later in data preprocessing step. All NaN values have you either imputed or interpolated using scikit.



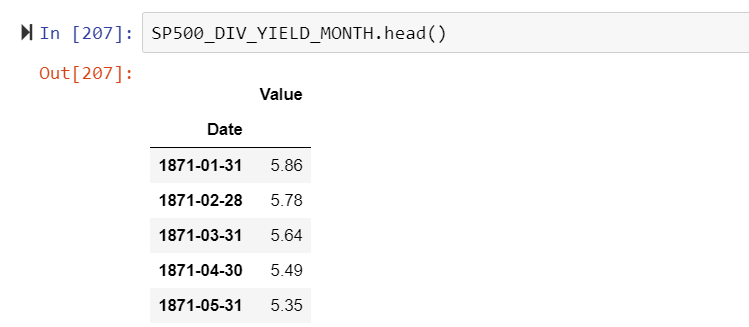
**Data API connection**-

Quandl API gives data in pandas dataframe format per dataset. I have merged all 36 columns on ‘Date’ timeseries. I would be using my personal key from my free account on Quandl data website where MULTPL provides API the following attributes for S&P500 index in time-series. All of the data combined together affects the price of S&P 500 index together with underlying constituent equity data. Underlying constituent equity data is out-of-scope for this project but would be interesting to include for further studies.

Snippet of API to fetch data from Quandl.



Sample dataframe from API-

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**Output data** - “S&P 500 Real Price by Month” (Target output) prediction.

**Input data-** 35 features available in the dataset which shows sales, P/E, growth, dividend ratios etc per month, quarter and Annually.

**Index name- S&P 500 Index**

**Asset class- Equities**

Characteristics of the dataset-

1. There are 36 data points.
2. Time-series data is split per month, per quarter and per year.
3. “S&P 500 Real Price by Month” is the target variable (y).
4. Earning yield, price to sales ratios and yeilds are available in time-series.
5. Data available is linear and ratios for many columns.
6. Columns like S&P 500 Sales by Year, S&P 500 Real Sales by Year have values much higher than other scaled down ratios which should be scaled down all together to avoid any biases.

|  |  |
| --- | --- |
| S&P 500 Dividend Yield by Month | MULTPL/SP500\_DIV\_YIELD\_MONTH |
| S&P 500 PE Ratio by Month | MULTPL/SP500\_PE\_RATIO\_MONTH |
| Shiller PE Ratio by Month | MULTPL/SHILLER\_PE\_RATIO\_MONTH |
| S&P 500 Earnings Yield by Month | MULTPL/SP500\_EARNINGS\_YIELD\_MONTH |
| S&P 500 Inflation Adjusted by Month | MULTPL/SP500\_INFLADJ\_MONTH |
| S&P 500 Price to Sales Ratio by Quarter | MULTPL/SP500\_PSR\_QUARTER |
| S&P 500 Dividend by Month | MULTPL/SP500\_DIV\_MONTH |
| S&P 500 Dividend by Year | MULTPL/SP500\_DIV\_YEAR |
| S&P 500 Dividend Growth by Year | MULTPL/SP500\_DIV\_GROWTH\_YEAR |
| S&P 500 Dividend Growth by Quarter | MULTPL/SP500\_DIV\_GROWTH\_QUARTER |
| S&P 500 Price to Book Value by Quarter | MULTPL/SP500\_PBV\_RATIO\_QUARTER |
| Shiller PE Ratio by Year | MULTPL/SHILLER\_PE\_RATIO\_YEAR |
| S&P 500 PE Ratio by Year | MULTPL/SP500\_PE\_RATIO\_YEAR |
| S&P 500 Dividend Yield by Year | MULTPL/SP500\_DIV\_YIELD\_YEAR |
| S&P 500 Price to Sales Ratio by Year | MULTPL/SP500\_PSR\_YEAR |
| S&P 500 Earnings Yield by Year | MULTPL/SP500\_EARNINGS\_YIELD\_YEAR |
| S&P 500 Price to Book Value by Year | MULTPL/SP500\_PBV\_RATIO\_YEAR |
| S&P 500 Inflation Adjusted by Year | MULTPL/SP500\_INFLADJ\_YEAR |
| S&P 500 Real Price by Month (Target output) | MULTPL/SP500\_REAL\_PRICE\_MONT |
| S&P 500 Sales by Year | MULTPL/SP500\_SALES\_YEAR |
| S&P 500 Sales Growth Rate by Year | MULTPL/SP500\_SALES\_GROWTH\_YEAR |
| S&P 500 Sales by Quarter | MULTPL/SP500\_SALES\_QUARTER |
| S&P 500 Real Sales Growth by Quarter | MULTPL/SP500\_REAL\_SALES\_GROWTH\_QUARTER |
| S&P 500 Sales Growth Rate by Quarter | MULTPL/SP500\_SALES\_GROWTH\_QUARTER |
| S&P 500 Real Sales Growth by Year | MULTPL/SP500\_REAL\_SALES\_GROWTH\_YEAR |
| S&P 500 Real Earnings Growth by Year | MULTPL/SP500\_REAL\_EARNINGS\_GROWTH\_YEAR |
| S&P 500 Real Sales by Year | MULTPL/SP500\_REAL\_SALES\_YEAR |
| S&P 500 Real Earnings Growth by Quarter | MULTPL/SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER |
| S&P 500 Earnings Growth Rate by Quarter | MULTPL/SP500\_EARNINGS\_GROWTH\_QUARTER |
| S&P 500 Real Sales by Quarter | MULTPL/SP500\_REAL\_SALES\_QUARTER |
| S&P 500 Earnings by Month | MULTPL/SP500\_EARNINGS\_MONTH |
| S&P 500 Book Value Per Share by Year | MULTPL/SP500\_BVPS\_YEAR |
| S&P 500 Earnings by Year | MULTPL/SP500\_EARNINGS\_YEAR |
| S&P 500 Earnings Growth Rate by Year | MULTPL/SP500\_EARNINGS\_GROWTH\_YEAR |
| S&P 500 Book Value Per Share by Quarter | MULTPL/SP500\_BVPS\_QUARTER |
| S&P 500 Real Price by Year | MULTPL/SP500\_REAL\_PRICE\_YEAR |
| Date | Timeseries since 1871 |

All column names of master df after joining/merging 36 dataframes from API-

Index(['Value\_SP500\_REAL\_PRICE\_MONTH', 'Value\_SP500\_DIV\_YIELD\_MONTH',  
 'Value\_SP500\_PE\_RATIO\_MONTH', 'Value\_SHILLER\_PE\_RATIO\_MONTH',  
 'Value\_SP500\_EARNINGS\_YIELD\_MONTH', 'Value\_SP500\_INFLADJ\_MONTH',  
 'Value\_SP500\_PSR\_QUARTER', 'Value\_SP500\_DIV\_MONTH',  
 'Value\_SP500\_DIV\_YEAR', 'Value\_SP500\_DIV\_GROWTH\_YEAR',  
 'Value\_SP500\_DIV\_GROWTH\_QUARTER', 'Value\_SP500\_PBV\_RATIO\_QUARTER',  
 'Value\_SHILLER\_PE\_RATIO\_YEAR', 'Value\_SP500\_PE\_RATIO\_YEAR',  
 'Value\_SP500\_DIV\_YIELD\_YEAR', 'Value\_SP500\_PSR\_YEAR',  
 'Value\_SP500\_EARNINGS\_YIELD\_YEAR', 'Value\_SP500\_PBV\_RATIO\_YEAR',  
 'Value\_SP500\_INFLADJ\_YEAR', 'Value\_SP500\_SALES\_YEAR',  
 'Value\_SP500\_SALES\_GROWTH\_YEAR', 'Value\_SP500\_SALES\_QUARTER',  
 'Value\_SP500\_REAL\_SALES\_GROWTH\_QUARTER',  
 'Value\_SP500\_SALES\_GROWTH\_QUARTER',  
 'Value\_SP500\_REAL\_SALES\_GROWTH\_YEAR',  
 'Value\_SP500\_REAL\_EARNINGS\_GROWTH\_YEAR', 'Value\_SP500\_REAL\_SALES\_YEAR',  
 'Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER',  
 'Value\_SP500\_EARNINGS\_GROWTH\_QUARTER', 'Value\_SP500\_REAL\_SALES\_QUARTER',  
 'Value\_SP500\_EARNINGS\_MONTH', 'Value\_SP500\_BVPS\_YEAR',  
 'Value\_SP500\_EARNINGS\_YEAR', 'Value\_SP500\_EARNINGS\_GROWTH\_YEAR',  
 'Value\_SP500\_BVPS\_QUARTER'],  
 dtype='object')

Joining and merging the data points together-

Join and/or merge all datasets on ‘Date’ column using left or outer join to create a master dataframe.

Ex- df = df.merge(

SHILLER\_PE\_RATIO\_MONTH,on='Date',how='left').merge(

SP500\_EARNINGS\_YIELD\_MONTH,on='Date',how='left').merge(

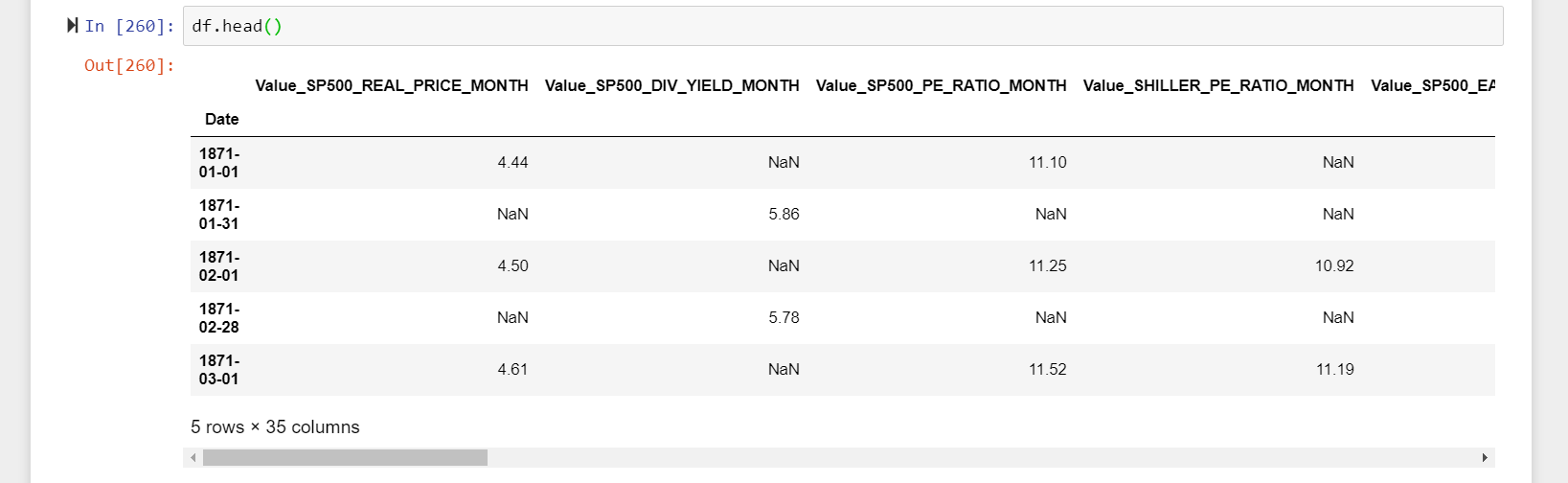
SP500\_INFLADJ\_MONTH,on='Date',how='left').merge(

SP500\_PSR\_QUARTER,on='Date',how='left').merge(

SP500\_DIV\_MONTH,on='Date',how='outer').merge(

SP500\_DIV\_YEAR,on='Date',how='left')

Master df preview snippet-



Times series available in ‘Date’ index is available for 1st of every month and last date of every month after joining all data variables. This introduced many missing values which needs to be handled.

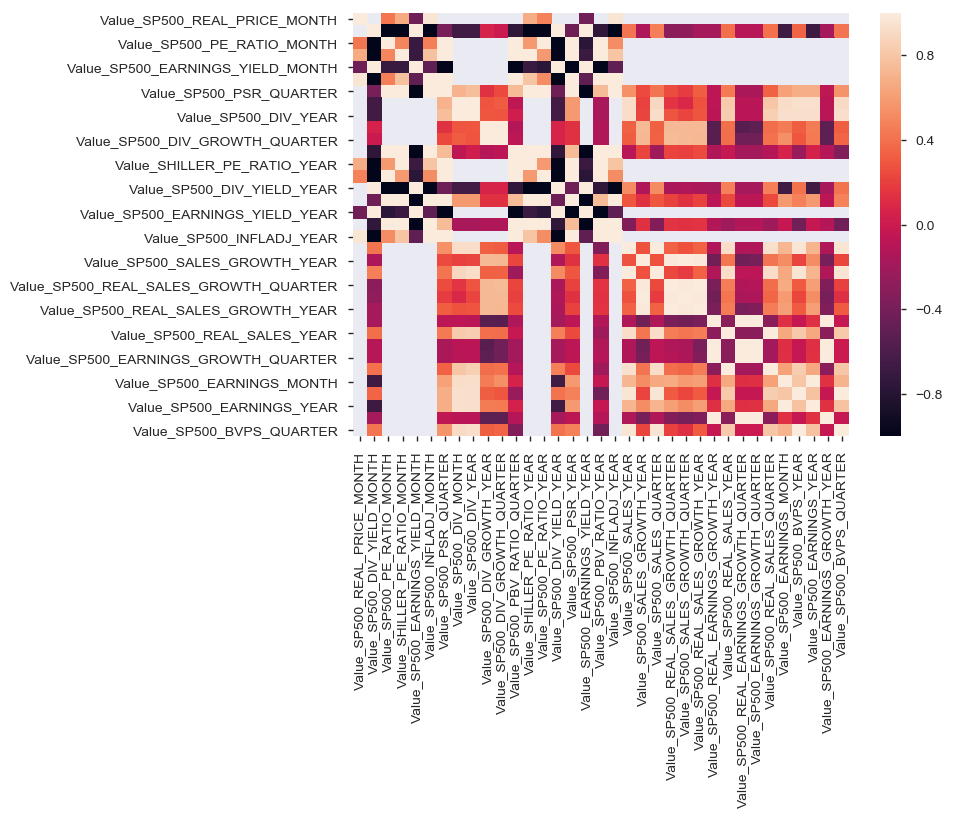
### **Exploratory Visualization**

After creating a master dataframe from API data variables, its time to impute and interpolate values for variables and then find out correlation between variables before and after imputation/interpolation.

**Master df correlation heatmap**-

#Correlation plot for all variable data values of API data in df.

sns.heatmap(df.corr(),annot=None,fmt='.2f',square=False)



#Pandas profiling of df

pandas\_profiling.ProfileReport(df)

There are lots of missing data in the master dataframe hence correlation between variables is 0 at many places.

Apply imputation on master dataframe-

Dataset info

|  |  |
| --- | --- |
| Number of variables | 36 |
| Number of observations | 3547 |
| Total Missing (%) | 0.0% |
| Total size in memory | 997.7 KiB |
| Average record size in memory | 288.0 B |

I have used SimpleImputer method from Scikit-learn library for replacing NaN values with ‘most frequent’ values used and this way I have LOCF’ed (last observation carried forward) the missing values in timeseries.

from sklearn.impute import SimpleImputer

#Create an imputation object

imputer\_most\_frequent= SimpleImputer(missing\_values=np.nan,strategy ='most\_frequent')

#Inject imputed values in the dataset.

df\_imputed = pd.DataFrame(imputer\_most\_frequent.fit\_transform(df))

df\_imputed.columns = df.columns

df\_imputed.index = df.index

pandas\_profiling.ProfileReport(df\_imputed)

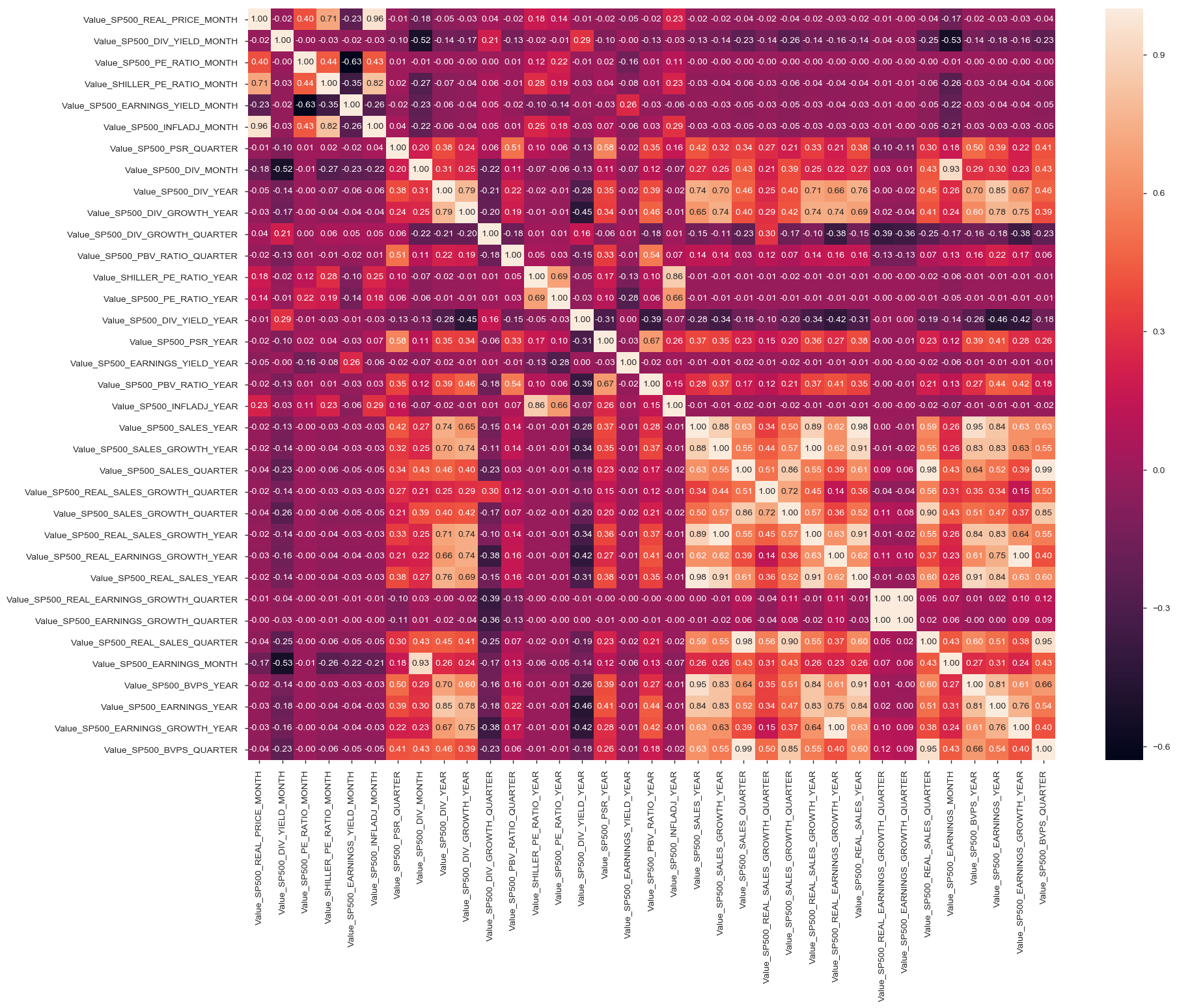
Imputed dataframe profiling-

* [Value\_SP500\_BVPS\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_BVPS_QUARTER) is highly correlated with [Value\_SP500\_REAL\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_QUARTER) (ρ = 0.95101)
* [Value\_SP500\_BVPS\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_BVPS_YEAR) is highly correlated with [Value\_SP500\_REAL\_SALES\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_YEAR) (ρ = 0.91377)
* [Value\_SP500\_EARNINGS\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_GROWTH_QUARTER) is highly correlated with [Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_EARNINGS_GROWTH_QUARTER) (ρ = 0.99834)
* [Value\_SP500\_EARNINGS\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_GROWTH_YEAR) is highly correlated with [Value\_SP500\_REAL\_EARNINGS\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_EARNINGS_GROWTH_YEAR) (ρ = 0.9994)
* [Value\_SP500\_EARNINGS\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_MONTH) is highly correlated with [Value\_SP500\_DIV\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_MONTH) (ρ = 0.93017)
* [Value\_SP500\_INFLADJ\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_INFLADJ_MONTH) is highly correlated with [Value\_SP500\_REAL\_PRICE\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_PRICE_MONTH) (ρ = 0.95881)
* [Value\_SP500\_PBV\_RATIO\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PBV_RATIO_YEAR) is highly skewed (γ1 = 23.541) **Skewed**
* [Value\_SP500\_PSR\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PSR_YEAR) is highly skewed (γ1 = 20.073) **Skewed**
* [Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_EARNINGS_GROWTH_QUARTER) is highly skewed (γ1 = 32.837) **Skewed**
* [Value\_SP500\_REAL\_SALES\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_GROWTH_YEAR) is highly correlated with [Value\_SP500\_SALES\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_GROWTH_YEAR) (ρ = 0.99905)
* [Value\_SP500\_REAL\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_QUARTER) is highly correlated with [Value\_SP500\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_QUARTER) (ρ = 0.98094)
* [Value\_SP500\_REAL\_SALES\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_YEAR) is highly correlated with [Value\_SP500\_REAL\_SALES\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_GROWTH_YEAR) (ρ = 0.91449)

#Correlation plot after imputation

plt.figure(figsize=(20,15))

sns.heatmap(df\_imputed.corr(),annot=True,fmt='.2f',square=False)



Replacing missing values using Linear Interpolation-

#Apply linear interpolation on the dataset.

df\_interpolate = df.interpolate(method='linear',axis=0,inplace=False,limit\_direction='both')

Correlation of variables after applying interpolation is much better than imputation.

Interpolated data profiling-

[Value\_SHILLER\_PE\_RATIO\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SHILLER_PE_RATIO_YEAR) is highly correlated with [Value\_SHILLER\_PE\_RATIO\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SHILLER_PE_RATIO_MONTH) (ρ = 0.98988)

* [Value\_SP500\_BVPS\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_BVPS_QUARTER) is highly correlated with [Value\_SP500\_BVPS\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_BVPS_YEAR) (ρ = 0.99959)
* [Value\_SP500\_BVPS\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_BVPS_YEAR) is highly correlated with [Value\_SP500\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_QUARTER) (ρ = 0.97758)
* [Value\_SP500\_DIV\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_GROWTH_QUARTER) is highly correlated with [Value\_SP500\_DIV\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_GROWTH_YEAR) (ρ = 0.99279)
* [Value\_SP500\_DIV\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_MONTH) is highly correlated with [Value\_SP500\_INFLADJ\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_INFLADJ_MONTH) (ρ = 0.91953)
* [Value\_SP500\_DIV\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_YEAR) is highly correlated with [Value\_SP500\_DIV\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_MONTH) (ρ = 0.99955)
* [Value\_SP500\_DIV\_YIELD\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_YIELD_YEAR) is highly correlated with [Value\_SP500\_DIV\_YIELD\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_YIELD_MONTH) (ρ = 0.97675)
* [Value\_SP500\_EARNINGS\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_GROWTH_QUARTER) is highly correlated with [Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_EARNINGS_GROWTH_QUARTER) (ρ = 0.99925)
* [Value\_SP500\_EARNINGS\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_GROWTH_YEAR) is highly correlated with [Value\_SP500\_REAL\_EARNINGS\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_EARNINGS_GROWTH_YEAR) (ρ = 0.99856)
* [Value\_SP500\_EARNINGS\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_MONTH) is highly correlated with [Value\_SP500\_INFLADJ\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_INFLADJ_YEAR) (ρ = 0.91628)
* [Value\_SP500\_EARNINGS\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_YEAR) is highly correlated with [Value\_SP500\_EARNINGS\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_MONTH) (ρ = 0.99515)
* [Value\_SP500\_EARNINGS\_YIELD\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_YIELD_YEAR) is highly correlated with [Value\_SP500\_EARNINGS\_YIELD\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_EARNINGS_YIELD_MONTH) (ρ = 0.98185)
* [Value\_SP500\_INFLADJ\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_INFLADJ_MONTH) is highly correlated with [Value\_SP500\_REAL\_PRICE\_MONTH](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_PRICE_MONTH) (ρ = 0.96798)
* [Value\_SP500\_INFLADJ\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_INFLADJ_YEAR) is highly correlated with [Value\_SP500\_DIV\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_DIV_YEAR) (ρ = 0.91992)
* [Value\_SP500\_PBV\_RATIO\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PBV_RATIO_YEAR) is highly correlated with [Value\_SP500\_PBV\_RATIO\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PBV_RATIO_QUARTER) (ρ = 0.99857)
* [Value\_SP500\_PSR\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PSR_YEAR) is highly correlated with [Value\_SP500\_PSR\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_PSR_QUARTER) (ρ = 0.9885)
* [Value\_SP500\_REAL\_SALES\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_GROWTH_QUARTER) is highly correlated with [Value\_SP500\_SALES\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_GROWTH_YEAR) (ρ = 0.97961)
* [Value\_SP500\_REAL\_SALES\_GROWTH\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_GROWTH_YEAR) is highly correlated with [Value\_SP500\_SALES\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_GROWTH_QUARTER) (ρ = 0.96655)
* [Value\_SP500\_REAL\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_QUARTER) is highly correlated with [Value\_SP500\_REAL\_SALES\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_YEAR) (ρ = 0.99503)
* [Value\_SP500\_SALES\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_GROWTH_QUARTER) is highly correlated with [Value\_SP500\_REAL\_SALES\_GROWTH\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_REAL_SALES_GROWTH_QUARTER) (ρ = 0.99013)
* [Value\_SP500\_SALES\_QUARTER](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_QUARTER) is highly correlated with [Value\_SP500\_SALES\_YEAR](http://localhost:8888/notebooks/MachineLearning/Capstone%20Project/Quandl%20S%20and%20P%20500%20index%20prices/S%26P500%20index%20price%20prediction.ipynb#pp_var_Value_SP500_SALES_YEAR) (ρ = 0.99942)

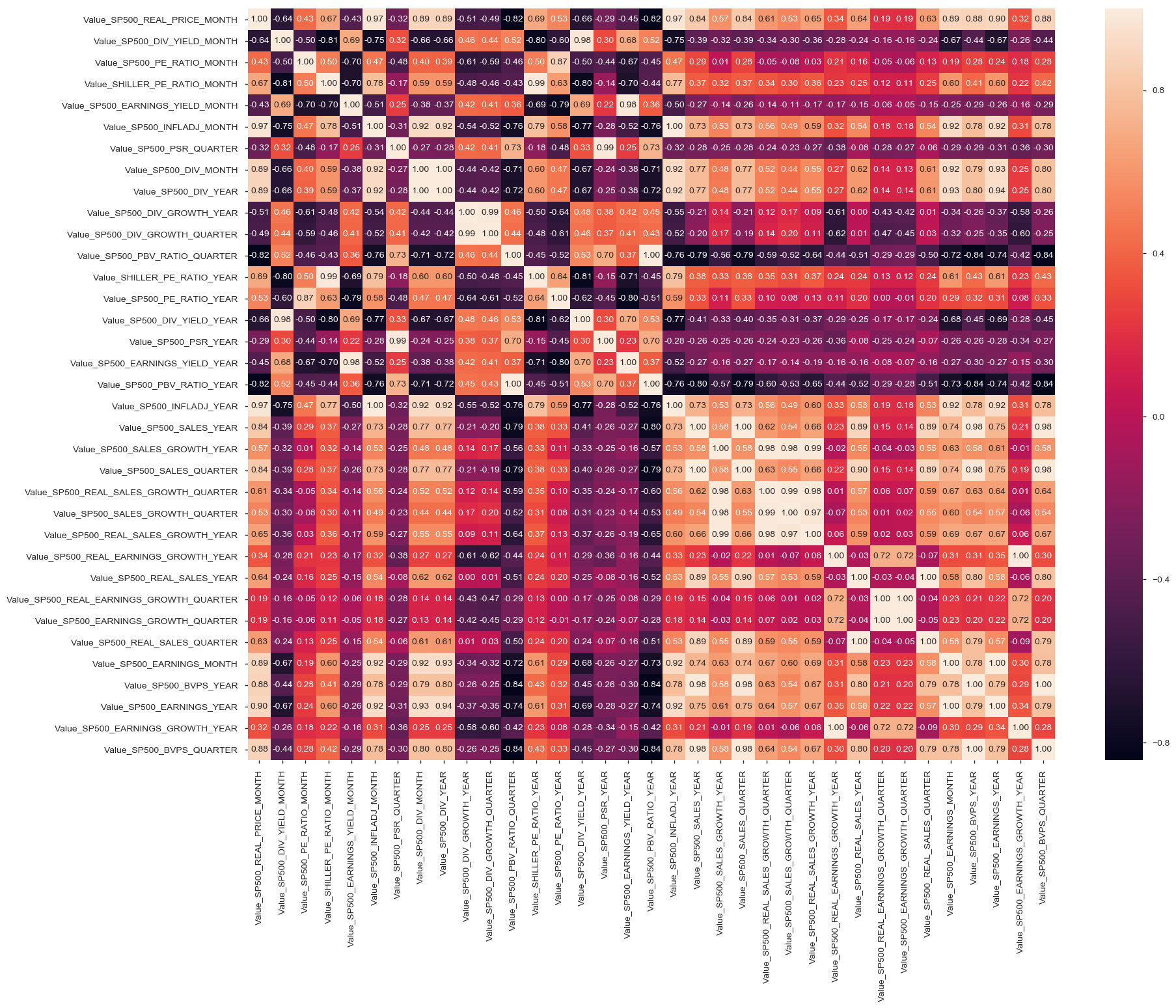
Correlation between variables/features after interpolation of missing values-

#Correlation heatmap plot after interpolation

plt.figure(figsize=(20,15))

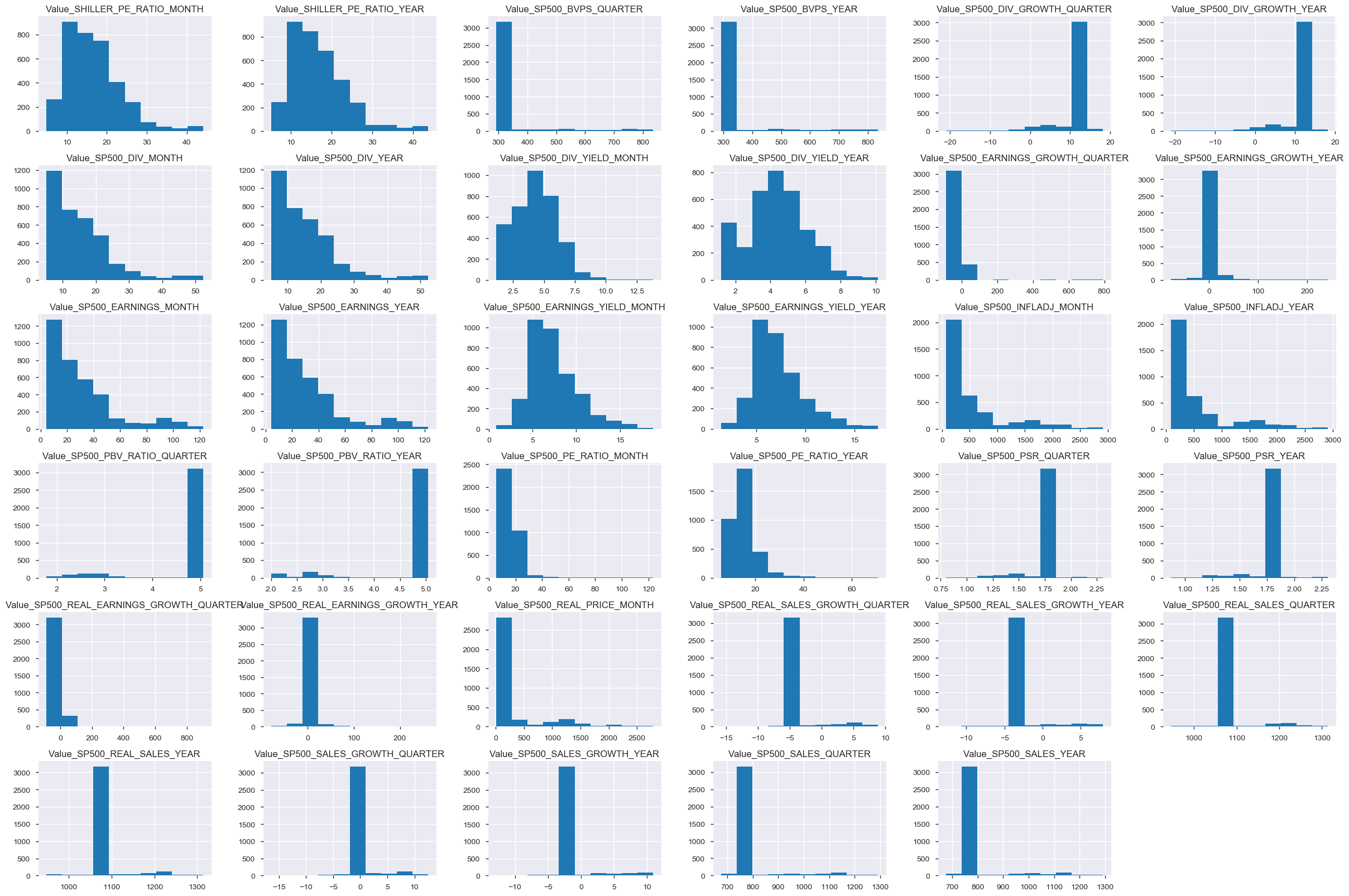
sns.heatmap(df\_interpolate.corr(),annot=True,fmt='.2f',square=False)

Correlation heatmap of variables is better than imputed correlation in interpolated data. There is strong relationship between many variables in the dataset which would help in feature engineering further on. Spearman correlation shows better results for interpolated data too.



Distribution of interpolated values for all variables-

Histogram shows distribution of values for interpolated values. For many variables, data distribution is skewed right except of a few where data is unimodal. This would affect fitting the regression predicted line during implementation of model. Features have to carefully selected.



Final analysis on interpolation and imputation datasets-

Linear Interpolation on missing values looks promising and there is better correlation between variables of the dataset. Imputation has not shown better correlation between variables. I would use interpolation dataframe for further analysis.

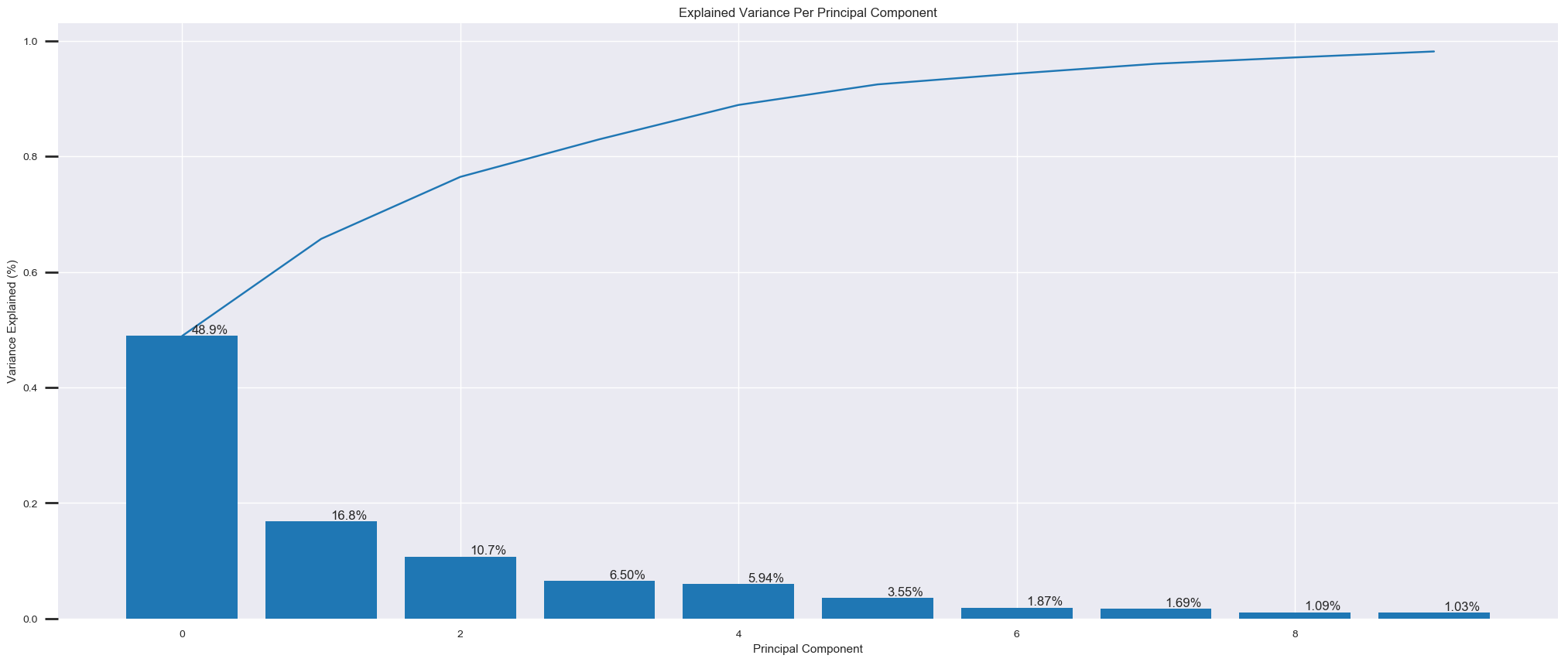
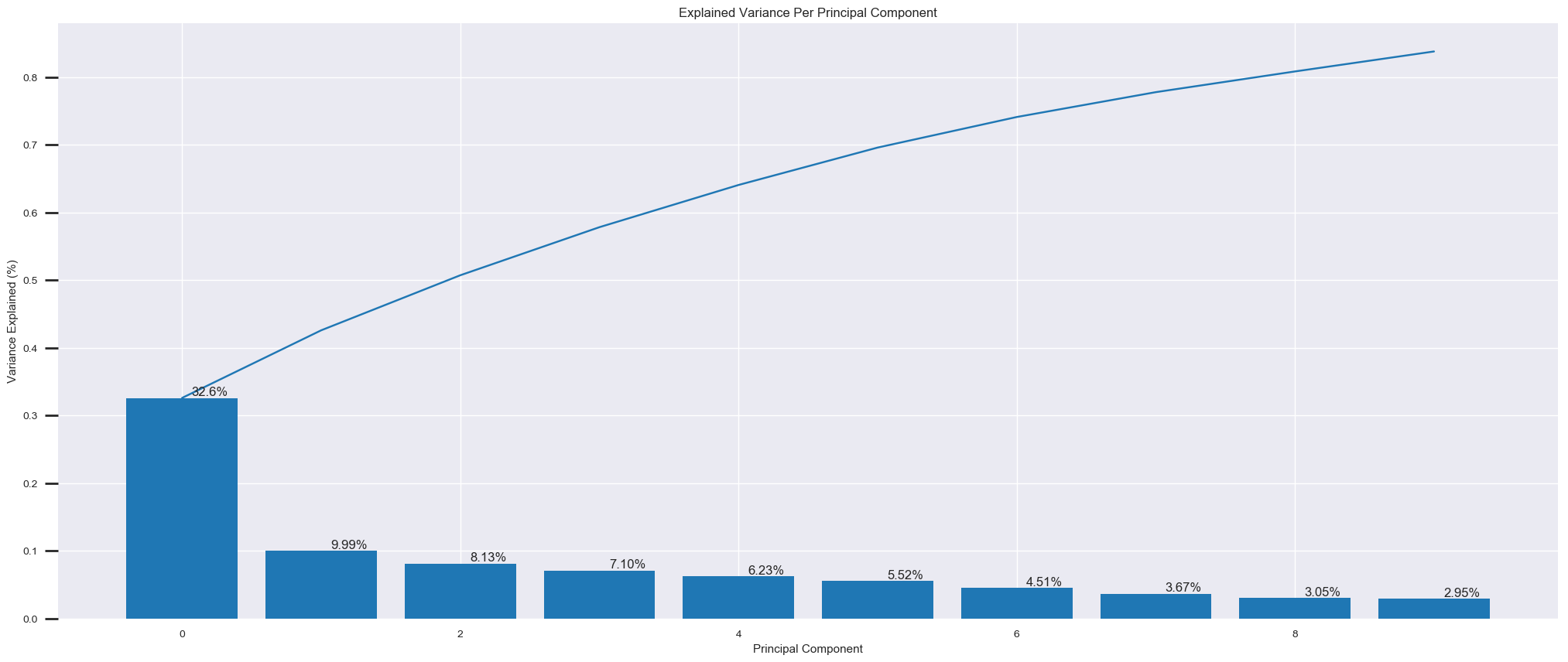
### **Algorithms and Techniques**

PCA- Principal Component Analysis

Principal component analysis (PCA) is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables (entities each of which takes on various numerical values) into a set of values of linearly uncorrelated variables called principal components.

I have scaled usig StandardScalar() all variables values from interpolated dataset before I used PCA to get an idea about variance of all 35 variables except for target variable 'Value\_SP500\_REAL\_PRICE\_MONTH' on interpolated dataset. I can use the variables from first cluster for modelling in Linear Regression, LSTM and fbProphet models.

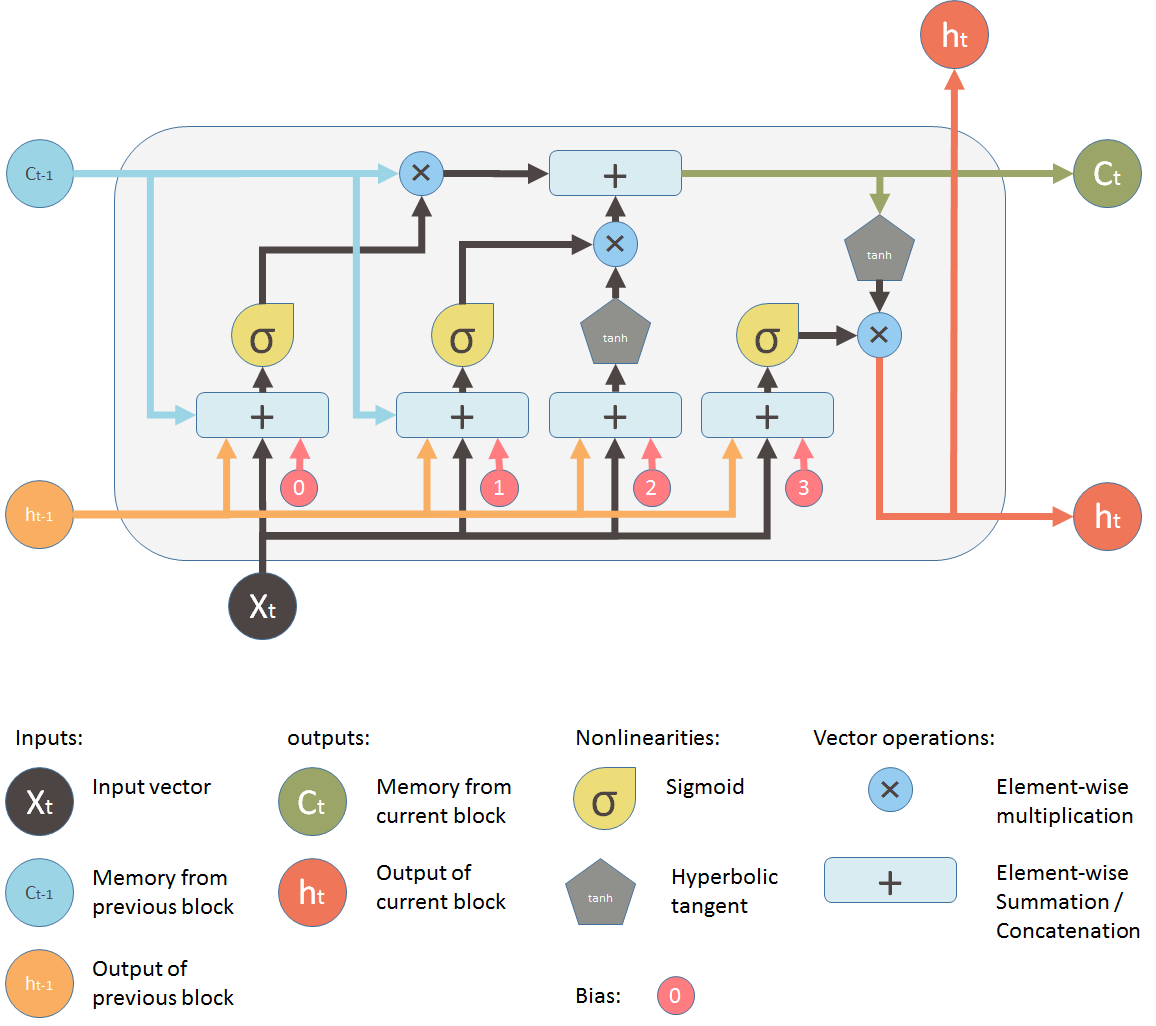
PCA cluster variance using interpolated dataset with 10 clusters shows strong variance after 1st and 2nd clusters. I would use it for modelling further.

PCA cluster variance using imputed dataset - there is not clear variance between clusters using imputed dataset. I would not use imputed dataset for modelling further on. 

Algorithms-

LSTM-

Neural Network model, with the type of model being a Recurring Neural Network (RNN). Under the RNN scope there are the LSTM algorithms that have recently been incorporated in various stock predicting algorithms and strategies because of their effectiveness compared to other neural algorithms. Long-term dependency is a problem that occurs in RNN when the network is in the need of making a prediction that requires context. In a regular RNN the need of understanding the context can be handled but this is dependent on how far back the memory needs to save the information for the context. LSTM’s have a chain structure and on the inside they operate using gates and layers of neural networks like other RNN approaches. The structure of the LSTM is constructed in a manner of a cell state that runs through the entire LSTM, the value is changed by the gates that have function by either allowing or disallowing data to be added to the cell state. There are also components by the name of gated cells that allow the information from previous LSTM outputs or layer outputs to be stored in them, this is where the memory aspect of LSTM’s kick in (Hochreiter and Schmidhuber, 1997).



LSTM references-

<https://medium.com/mlreview/understanding-lstm-and-its-diagrams-37e2f46f1714>

<https://en.wikipedia.org/wiki/Long_short-term_memory>

<https://medium.com/@huangkh19951228/predicting-cryptocurrency-price-with-tensorflow-and-keras-e1674b0dc58a>

<https://medium.com/mlreview/a-simple-deep-learning-model-for-stock-price-prediction-using-tensorflow-30505541d877>

fbProphet-

**How Prophet works-**

At its core, the Prophet procedure is an additive regression model with four main components:

* A piecewise linear or logistic growth curve trend. Prophet automatically detects changes in trends by selecting changepoints from the data.
* A yearly seasonal component modeled using Fourier series.
* A weekly seasonal component using dummy variables.
* A user-provided list of important holidays.

References-

<https://research.fb.com/prophet-forecasting-at-scale/>

<https://towardsdatascience.com/analysis-of-stock-market-cycles-with-fbprophet-package-in-python-7c36db32ecd0>

### **Benchmark**

Linear regression model

The term "linearity" in algebra refers to a linear relationship between two or more variables. If we draw this relationship in a two dimensional space (between two variables, in this case), we get a straight line. Linear regression is a basic and commonly used type of predictive analysis. The overall idea of regression is to examine which variables in particular are significant predictors of the outcome variable, and in what way do they–indicated by the magnitude and sign of the beta estimates–impact the outcome variable? These regression estimates are used to explain the relationship between one dependent variable and one or more independent variables. The simplest form of the regression equation with one dependent and one independent variable is defined by the formula y = c + b\*x, where y = estimated dependent variable score, c = constant, b = regression coefficient, and x = score on the independent variable.

Ref- <https://en.wikipedia.org/wiki/Linear_regression>

<https://stackabuse.com/linear-regression-in-python-with-scikit-learn/>

<https://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LinearRegression.html>

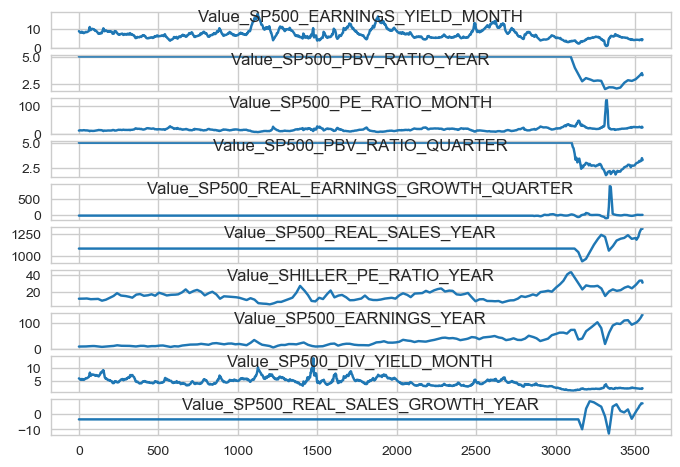
I have considered simple linear regression model as benchmark model. It is easy and simple to understand a regression problem with this model for prediction, forecasting purposes. I would train the model with 90% of data and test on 10% because the real price has increased in the past few years logarithmically. As mentioned by me, I couldnt find any available benchmark model for similar dataset for S&P 500 index price.

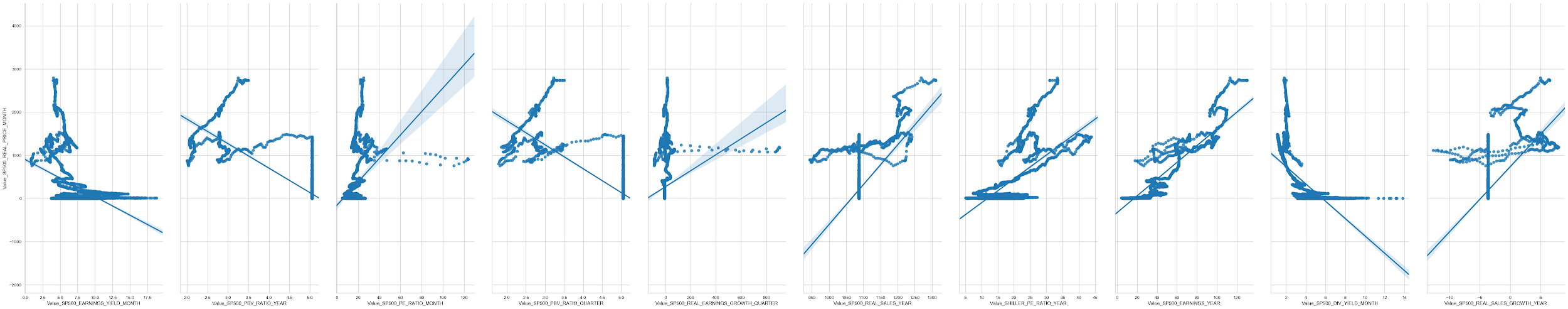
Benchmark results from the selected monthly variables dataset shows high mean square error. Even after working with features through PCA and selecting monthly variables, results from Linear Regression are not good. MSE is too high.

Plotting the Least Squares Line

Best observed high variance features Vs target label 'Value\_SP500\_REAL\_PRICE\_MONTH' to understand linear corelation.This is to find colinearity between features and the prediction line for selected set of features. Predicted line would try to fit with linear regression model through the feature data points.The dataset here is very imbalanced and non linear which makes it different to predict a linear line with optimum coefficients and intercept.

PCA components timeseries plot of interpolated dataset.





From the above pairplot it is clear that the data is unbalanced and skewed and not linear in nature. Predicted linear regression line has different slopes with respect to PCA components.

Reference-

<https://en.wikipedia.org/wiki/Linear_regression>

## **III. Methodology**

### **Data Preprocessing**

split and slicing, PCA components.

Scaling-

I have used Standard Scaling function from Scikit-learn library.

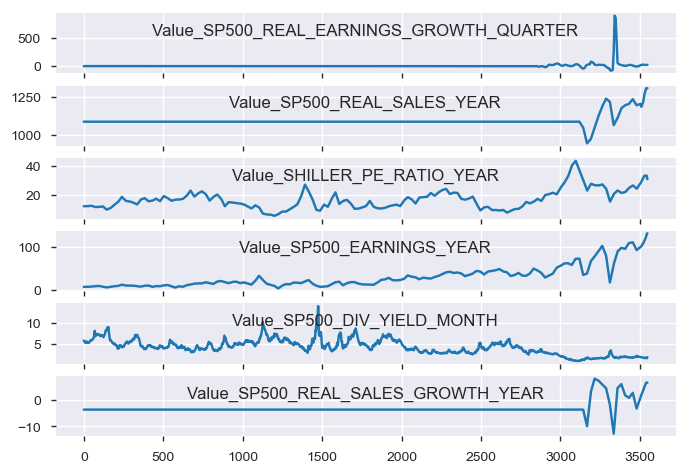
from sklearn.preprocessing import StandardScaler

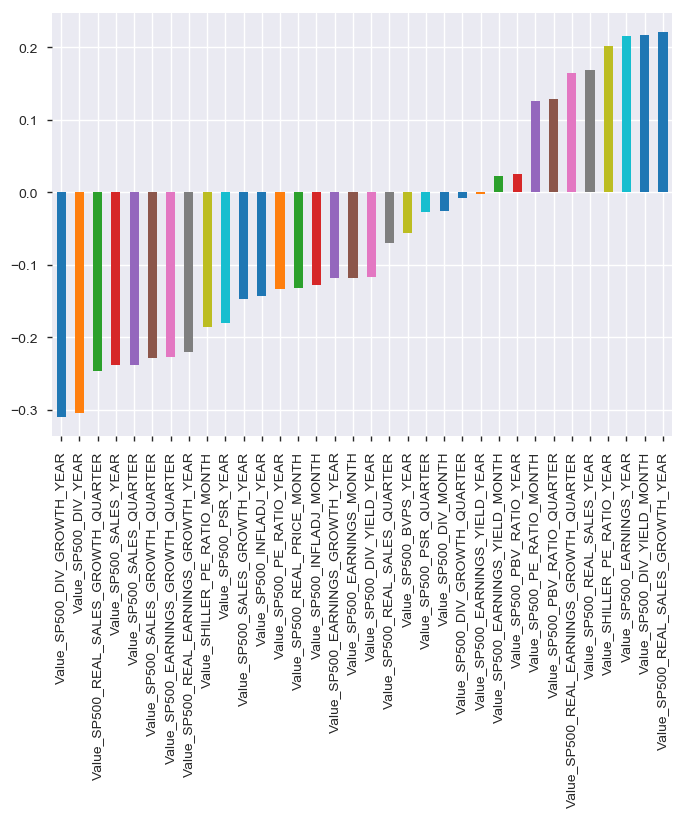
PCA components-

I have calculated and shown sorted weights of components in PCA cluster with highest variance. Principal compoments are -

['Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER',  
 'Value\_SP500\_REAL\_SALES\_YEAR',  
 'Value\_SHILLER\_PE\_RATIO\_YEAR',  
 'Value\_SP500\_EARNINGS\_YEAR',  
 'Value\_SP500\_DIV\_YIELD\_MONTH',  
 'Value\_SP500\_REAL\_SALES\_GROWTH\_YEAR']

Timeseries of PCA features for interpolated dataset.





Plot of all principal components for interpolated dataset

Split and slicing-

I have split the interpolated dataset into a subset dataset with selected variable labels for LSTM and Linear regression purpose but I did not get expected results even if I use PCA components or monthly variables from the dataset. I split the 98% for training and 2% for prediction.

df\_PCA\_features = df\_interpolate.loc[:,['Value\_SP500\_REAL\_PRICE\_MONTH',

'Value\_SP500\_DIV\_YIELD\_MONTH',

'Value\_SP500\_PE\_RATIO\_MONTH',

'Value\_SHILLER\_PE\_RATIO\_MONTH',

'Value\_SP500\_EARNINGS\_YIELD\_MONTH',

'Value\_SP500\_INFLADJ\_MONTH',

'Value\_SP500\_EARNINGS\_MONTH','Value\_SP500\_PSR\_QUARTER','Value\_SP500\_SALES\_QUARTER',

'Value\_SP500\_REAL\_SALES\_GROWTH\_QUARTER','Value\_SP500\_REAL\_EARNINGS\_GROWTH\_QUARTER']]

df\_PCA\_features.shape

(3548, 11)

Training and Test data size-

Training and Test dataset is of size 3477 & 71  
Features size of X\_train and training target Y\_train shape is (3477, 10) & (3477, 1)  
Features size of X\_test and Test target Y\_test shape is (71, 10) & (71, 1)  
Training dataset is converted to np.array with size (3477, 10) & (3477, 1)  
Test dataset is converted to np.array with size (71, 10) & (71, 1)

I split the interpolated dataset chronologically to avoid look-ahead bias in the timeseries. Index price values for last 71 months (about 6 years looking back) shows a steep increase in real price curves. I changed the dataframe values to np.array in preprocessing step before feeding it to LSTM network even though it is not required because LSTM accepts pandas dataframe as input to the network.

### **Implementation**

LSTM(Long Short-term Memory)

I have designed the network with Sequential model, 512 as input to hidden LSTM layers. LSTM Input layer has 3477 samples, 1 timesteps and 10 features. Inputs to LSTM layer should in format (n\_samples, timesteps, n\_features).

Then I have added dropout of 20%. A network of 512 neurons is connected with one hidden layer which would normalize the activations of the input layer at each batch, i.e. applies a transformation that maintains the mean activation close to 0 and the activation standard deviation close to 1.

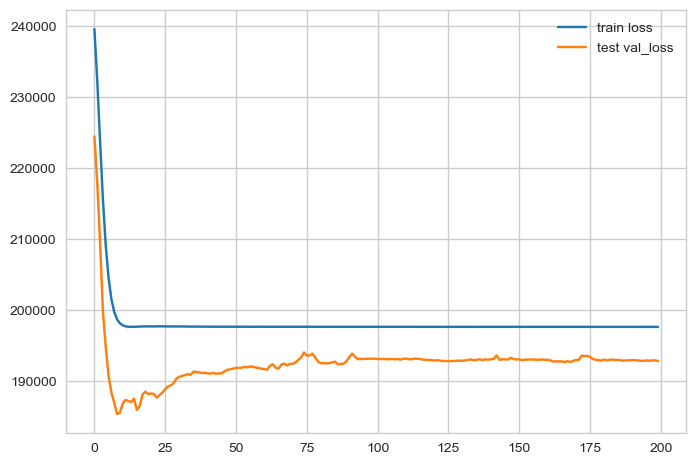
The cell state is kind of like a conveyor belt. It runs straight down the entire chain, with only some minor linear interactions. It’s very easy for information to just flow along it unchanged. The LSTM does have the ability to remove or add information to the cell state, carefully regulated by structures called gates. Gates are a way to optionally let information through. They are composed out of a sigmoid neural net layer and a pointwise multiplication operation.

I used ‘relu’ activation function before Dense model and ‘Softmax’ activation function in output as standard configuration for LSTM models. Checkpoint would save the model for best results.

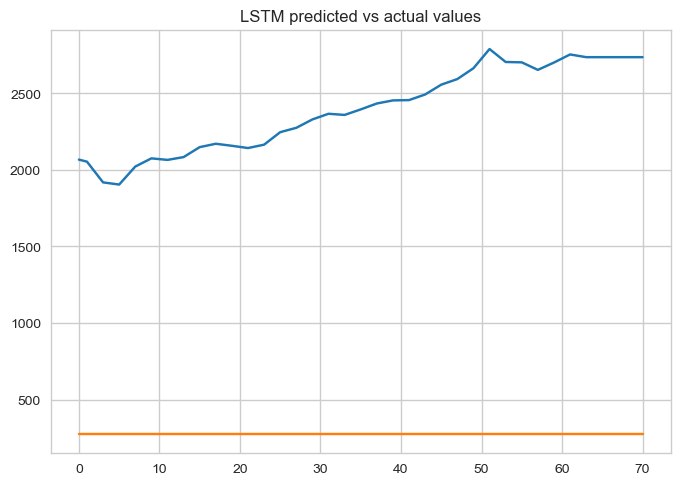
The model will be fit for 200 training epochs with a batch size of 100. Internal state of the LSTM in Keras is reset at the end of each batch, so an internal state that is a function of a number of days may be helpful.Finally, we keep track of both the training and test loss during training by setting the validation\_data argument in the fit() function. At the end of the run both the training and test loss are plotted.

**Evaluate Model**

After the model is fit, we can forecast for the entire test dataset. We combine the forecast with the test dataset and invert the scaling. We also invert scaling on the test dataset with the expected pollution numbers. With forecasts and actual values in their original scale, we can then calculate an error score for the model. In this case, we calculate the Root Mean Squared Error (RMSE) that gives error in the same units as the variable itself.



Train data vs test validation loss plot



Predicted price of S&P 500 index was way below the actual prices for last 71 months using PCA variables with highest variance or with selected features with monthly ratios.

**Description of parameters used in LSTM model-**

LSTM-

Neural networks like Long Short-Term Memory (LSTM) recurrent neural networks are able to almost seamlessly model problems with multiple input variables.LSTMs are explicitly designed to avoid the long-term dependency problem. All recurrent neural networks have the form of a chain of repeating modules of neural network. In standard RNNs, this repeating module will have a very simple structure, such as a single tanh layer. The key to LSTMs is the cell state, the horizontal line running through the top of the diagram. The LSTM does have the ability to remove or add information to the cell state, carefully regulated by structures called gates.

This is a great benefit in time series forecasting, where classical linear methods can be difficult to adapt to multivariate or multiple input forecasting problems.

Ref- <http://colah.github.io/posts/2015-08-Understanding-LSTMs/>

<https://machinelearningmastery.com/make-predictions-long-short-term-memory-models-keras/>

Activation function- ‘relu’- this is a popular activation function in deep neural networks because it has better gradient propagation, fewer [vanishing gradient](https://en.wikipedia.org/wiki/Vanishing_gradient_problem) problems compared to sigmoidal activation functions that saturate in both directions. Rectified linear units, compared to [sigmoid function](https://en.wikipedia.org/wiki/Sigmoid_function) or similar activation functions, allow for faster and effective training of deep neural architectures on large and complex datasets.

Ref- <https://www.reddit.com/r/MLQuestions/comments/6cadgx/do_relu_activation_functions_make_the_lstm/>

Loss function = ‘mse’ - The goal is to predict a single continuous value instead of a discrete label of the index price with given data. The network ends with a Dense without any activation because applying any activation function like sigmoid will constrain the value to 0~1 and we don't want that to happen.The mse loss function, it computes the square of the difference between the predictions and the targets, a widely used loss function for regression tasks.

Ref- <https://www.dlology.com/blog/how-to-choose-last-layer-activation-and-loss-function/>

Optimizer='adam' - Benefits of adam optimiser are-

* Computationally efficient.
* Little memory requirements.
* Invariant to diagonal rescale of the gradients.
* Well suited for problems that are large in terms of data and/or parameters.

Adam realizes the benefits of both AdaGrad and RMSProp.Instead of adapting the parameter learning rates based on the average first moment (the mean) as in RMSProp, Adam also makes use of the average of the second moments of the gradients (the uncentered variance).Specifically, the algorithm calculates an exponential moving average of the gradient and the squared gradient, and the parameters beta1 and beta2 control the decay rates of these moving averages.

Ref- <https://machinelearningmastery.com/adam-optimization-algorithm-for-deep-learning/>

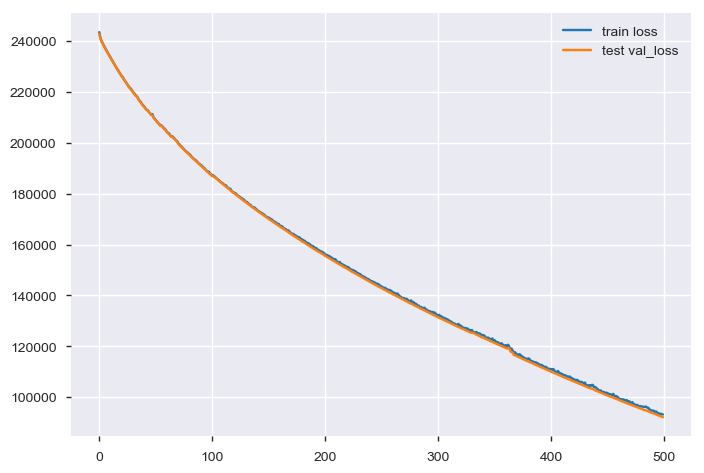
Difficulties with LSTM-

LSTM network is difficult to create because in my case Dense layer does not take more than 1 estimator and I could understand why. I had difficulties with defining input size and defining more hidden layers with LSTM network. The network I could build is very basic and minimum functional neural network.

### **Refinement**

I removed activation function ‘softmax’ after dense fully connected network because it was acting as stop gate in LSTM. Accuracy improved after it. I removed BatchNormalization() as normalization was not helping to improve results. This is a small dataset to apply data normalization in batches. I tried to refine LSTM model with different combinations of features but didn’t get expected results. LSTM model could be refined with multiple hidden layers and different activation functions. There is clearly huge scope of improvements with better business knowledge on features and LSTM expertise to make the neural network train as much better.

Training data and validation data loss after refinement.



For refinement I tried fbProphet model and the results are not better either. fbProphet model takes 2 labels in a dataframe- time-series and forecast label.

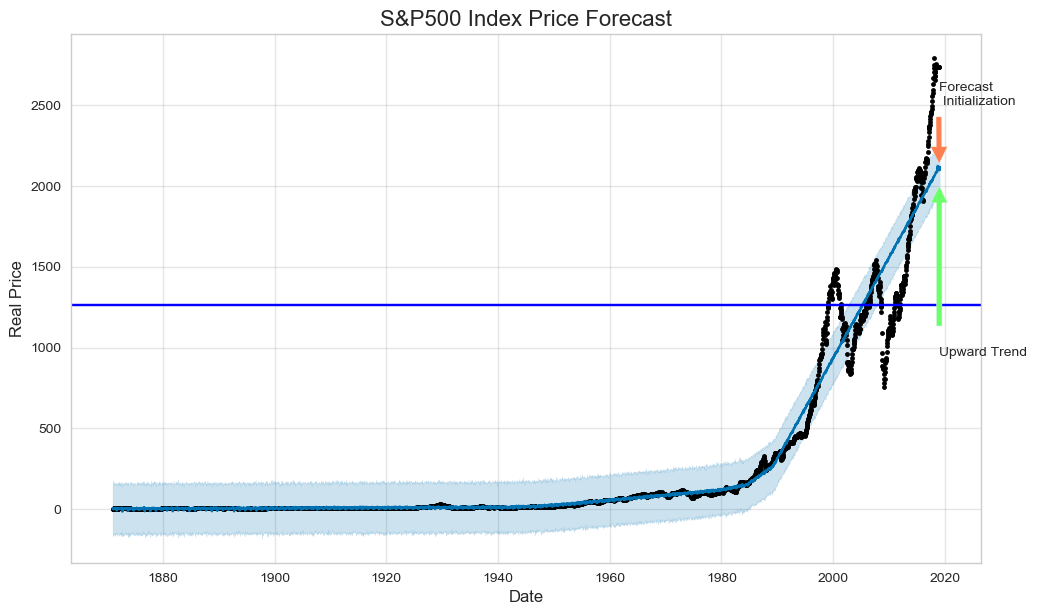
from fbprophet import Prophet

#Create future dates

future\_dates = fb.make\_future\_dataframe(periods=30)

#Predict prices for future dates

future\_price = fb.predict(future\_dates)



Forecasted price using fbProphet-

future\_price[['ds', 'yhat', 'yhat\_lower', 'yhat\_upper']].tail()

ds yhat yhat\_lower yhat\_upper

3573 2019-01-26 2104.546587 1937.262720 2262.138696

3574 2019-01-27 2109.010824 1954.873221 2261.450394

3575 2019-01-28 2109.505319 1951.637642 2271.802746

3576 2019-01-29 2111.732478 1958.432705 2263.845634

3577 2019-01-30 2115.552914 1957.799005 2267.874511

## **IV. Results**

### **Model Evaluation and Validation**

LSTM model evaluation-

Final parameter could be better with multilevel LSTM hidden layers. But still i think LSTM is not better for this kind of autoregression problem. ARIMA models or other autoregression problem could be better for this kind of time-series problem. Must be tested.

Means Square Error between Y\_test and prediction values is : 1586328991228.7246

R2 score between Y\_test adn prediction value is : -73.4024904609074

Results from training-

- 2s - loss: 195472.0549 - acc: 0.0000e+00 - val\_loss: 182259.5592 - val\_acc: 0.0000e+00  
Epoch 172/200  
 - 2s - loss: 195474.6800 - acc: 0.0000e+00 - val\_loss: 182338.4478 - val\_acc: 2.8760e-04  
Epoch 173/200  
 - 2s - loss: 195510.6922 - acc: 0.0000e+00 - val\_loss: 182226.1746 - val\_acc: 0.0000e+00  
Epoch 174/200  
 - 2s - loss: 195486.7277 - acc: 0.0000e+00 - val\_loss: 182274.0971 - val\_acc: 2.8760e-04

Linear Regression evaluation-

Mean squared error: 1076172.6990871658  
Root Mean squared error: 1037.3874392372243  
Variance R2 score: -1.9382920775190278

LSTM vs Linear Regression comparison-

LSTM mse = 1586328991228.7246 Linear regression mse = 1076172.6990871658  
It is clear that linear regression is better model in this scenario given the parameters I have used to define LSTM. mse is much larger for LSTM than linear regression model. Predictions are underfitting.

fbProphet evaluation-

Using this model i have predicted the price for the time-series to evaluate if fbProphet can predict this autoregression time-series dataset any better. It seems be forecasting within an acceptable range.

ds yhat yhat\_lower yhat\_upper

3573 2019-01-26 2104.546587 1937.262720 2262.138696

3574 2019-01-27 2109.010824 1954.873221 2261.450394

3575 2019-01-28 2109.505319 1951.637642 2271.802746

3576 2019-01-29 2111.732478 1958.432705 2263.845634

3577 2019-01-30 2115.552914 1957.799005 2267.874511

Evaluations of both models are very bad quality and results should not be trusted by any means. This dataset and project requires in depth evaluation and may be additional features for expected results.

### **Justification**

This dataset and project required in depth review of dataset and greater tuning of LSTM network. I could not find any justification or clear answer to why predicted values are way less than actual leading to huge error, 0 accuracy and high training/validation loss.

Both benchmark results from Linear regression model and LSTM are of bad quality which could be because of skewed dataset, interpolation of missing values or further model tuning required. I could also think of using separate models for monthly, quarterly and yearly time-series in this given dataset for regression and then build the final model on top of three models.

## **V. Conclusion**

### **Free-Form Visualization**

Conclusion of this project-

Problem statement for this project is to predict S&P 500 index price in the near future based on historical variables linked with S&P Index price. Dataset i selected is available for free on Quandl API. I collected 36 variables and selected Real monthly price as target label to train the supervised model.

36 Variables have monthly, quarterly ratios, prices, dividend yields etc. since 1871 but not all variables are available since 1871. A few variables are available from 1990 or early 2000s. To join and merge all 36 variables into one master dataset introduced NaN values quarterly and yearly variables in the monthly time series which means that I have impute values for LSTM. Hence I used imputation and linear interpolation methods to fill in the missing values in the time-series which is also called as LOCF’ed (last observation carried forward).

PCA analysis on scaled features using StandardScalar() shows that interpolated dataset has variance in first and second clusters of features from which i have selected 6 features with top variance. But LSTM result were underfitting with PCA features so I selected 10 monthly features instead.

Linear Regression model is the benchmark to predict the index price but dataset seems to be too skewed and unbalance hence the results are way underfitting and lead to huge errors.

I used sequential linear stack of layers for LSTM neural network, 512 neurons in the input hidden layer, dropout of 20%, relu activation function and dense net in output layer. Model architecture is very simple and could be further detailed with multiple layers of LSTM and positive and negative gates as activation functions. But there are challenges with the dataset interpolated values do not form a linear regression line.Following image shows the workflow of the project.



**Project Workflow**

fbProphet is easy to use and helpful for auto-regression problems. I used it for experimenting with the dataset to verify if this auto-regression model works on the dataset at all. The model could predict but was not close to the actual.

S&P 500 index price could not be predicted as expected partly due to dataset (possibly) and also because I could not train LSTM correctly. This project requires better features and more data to forecast the price correctly.

LSTM does not appear to be suitable for autoregression problems possibly. It seems likely though. ARIMA models could work on this dataset. Need to test.

Ref- <https://en.wikipedia.org/wiki/Autoregressive_model>

### **Reflection**

My reflections on this project is that dataset is very unbalanced and skewed and features are not clearly related with each other. It is difficult to find any patterns in the dataset which links with the real price of index. More work on correcting the dataset is required and feature engineering requires more time and business knowledge. Business knowledge is clearly missing in this project.

Feature engineering has been challenging with this dataset specially with skewed variables and missing values in time-series.

### **Improvement**

Handling missing values might make the difference in predicting the index price in future. Also, constituent data of underlying stocks would help in selecting correct features too. Features like, trading volume, high price, low price, open price, closing price of underlying constituent stocks would definitely help in feature engineering.

Different model strategies might work on different frequency of variables. Dropping variables which have many missing values could help as well. Moving average models could work in this case if some features are assumed to be stationary series among the variables.